MAGDI: Structured Distillation of Multi-Agent Interaction Graphs Improves Reasoning in Smaller Language Models

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Abstract

Multi-agent interactions between Large Language Model (LLM) agents have shown major improvements on diverse reasoning tasks. However, these involve long generations from multiple models across several rounds, making them expensive. Moreover, these multi-agent approaches fail to provide a final, single model for efficient inference. To address this, we introduce MAGDI, a new method for structured distillation of the reasoning interactions between multiple LLMs into smaller LMs. MAGDI teaches smaller models by representing multiagent interactions as graphs, augmenting a base student model with a graph encoder, and distilling knowledge using three objective functions: next-token prediction, a contrastive loss between correct and incorrect reasoning, and a graph-based objective to model the interaction structure. Experiments on seven widely-used commonsense and math reasoning benchmarks show that MAGDI improves smaller models' reasoning, outperforming several methods that distill from a single teacher and multiple teachers. Moreover, MAGDI also shows an order of magnitude higher efficiency over its teachers. We conduct extensive analyses to show that MAGDI (1) enhances the generalizability to out-of-domain tasks, (2) scales positively with the size and strength of the base student model, and (3) obtains larger improvements when applying self-consistency – an inference technique that relies on model diversity.¹

1 Introduction

Debate and dialogue are natural ways to improve reasoning: we form our best ideas not in isolation, but by refining and discussing them with others. Similarly, we can improve Large Language Models (LLMs) – which often exhibit impressive multi-step reasoning capabilities (Wei et al., 2022; Kojima

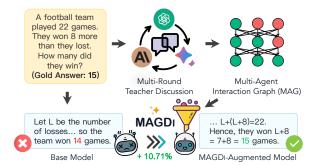


Figure 1: Overview of our distillation method. Given a reasoning problem, multiple teacher-LLMs engage in a multi-round discussion, leading to the generation of a multi-agent interaction graph (MAG). MAGDI distills knowledge from these MAG into a base student model.

et al., 2022) – by allowing multiple LLM instances to interact in a discussion (Du et al., 2023; Chen et al., 2023b; Wu et al., 2023). These interactive frameworks enable each agent to iteratively refine its reasoning by obtaining feedback from others, thereby leading to a better consensus at the end of multiple interaction rounds.

Discussion frameworks are typically built on top of proprietary models, e.g., GPT-4, Bard, Claude, etc., which can act as general conversational agents, handle long contexts, and follow instructions (Bubeck et al., 2023). However, these models are expensive, especially when used in multi-round interactions, which require numerous long-token length inference calls to the underlying LLMs. Moreover, these frameworks do not result in a final, joint model that can then be directly used for inference and instead requires invoking all interacting LLMs at test time. To reduce this cost and train a small, affordable yet capable model, we tackle the problem of teaching reasoning to smaller language models via structured distillation of the interactions between multiple stronger teacher models. Specifically, we develop a structured distillation method, Multi-Agent Interaction Graphs Distillation (MAGDI), that enables a stu-

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¹Code/data: https://github.com/dinobby/MAGDi.

dent model to learn from multi-teacher interactions, with the goal of developing a performant and efficient standalone alternative to expensive multiagent setups. On seven benchmarks in both commonsense and math reasoning, we find increasing improvements over distillation baselines as we incorporate more levels of teacher interactions.

To learn from teacher interaction structure, we represent it in Multi-Agent Interaction Graphs (MAG), a graph-based encoding of multi-agent interactions. Concretely, a MAG is a directed acyclic graph (DAG) wherein each node represents an agent's generation in a discussion round, annotated with a binary label indicating whether the answer is correct. The edges denote the discussion's structure, indicating which previous turns agents are responding to. Given a reasoning problem, MAGs capture rich knowledge of (1) diverse pre- and postinteraction correct reasoning chains generated by different LLMs, (2) challenging incorrect reasoning chains generated by different LLMs that are refined over interaction rounds, and (3) an *iterative* and structured (graph-based) interaction process that enables this refinement of model reasoning. We capture all this knowledge via the following four levels of MAG components, which are then used in our distillation method, MAGDI.

Level 1: Learning from multiple teachers. The student learns from the correct reasoning of *multiple* teachers, rather than one.

Level 2: Learning from teacher interactions. The student learns from both pre- and *post-interaction* data between multiple teachers.

Level 3: Learning from negative reasoning. The student additionally distills from *negative or incorrect* reasoning from the teacher models.

Level 4: Learning from structure. The student learns from the output and *graph-structure* of teacher LLM interactions.

Note that each level builds on the prior levels, motivating our main **Research Question:** *How can we effectively distill from diverse teacher interactions into a smaller, efficient student model across increasing levels of interaction structure, also demonstrating scalability and generalizability?*

These levels also shape MAGDI, our structured distillation method. MAGDI enables a student model to learn from our graph-structured interaction data (MAGs), with the goal of developing a performant and efficient standalone substitute to costly multi-agent systems. We first construct a training

dataset of MAGs from a high-performing multiagent discussion framework (Chen et al., 2023b), featuring discussions between three API-based LLMs: GPT-4, Bard, and Claude2. We then develop student models augmented with a Graph Neural Network (GNN) for learning structure-aware representations of positive (correct) and negative (incorrect) reasoning chains and fine-tune them on MAG data. MAGDI's three fine-tuning objectives are aligned to the four levels: (1) next-token prediction (Levels 1-2), (2) a contrastive loss between correct and incorrect reasoning (Level 3), and (3) a graph-based node classification loss (Level 4). These objectives capture all useful signals in MAGs (i.e., teachers' correct and incorrect reasoning and the conversation structure).

We evaluate MAGDI's effectiveness on seven widely-used commonsense (StrategyQA, CommonsenseQA, ARC-c, BoolQ) and math (GSM8K, MATH, SVAMP) reasoning benchmarks, consistently establishing the following findings:

- **Multi-teacher improves student performance.** Compared to distilling from a single teacher, distilling from *multiple teachers* improves student model's performance (Level 1).
- The value of teacher interactions: Distilling from the *post-interaction* outputs of teachers further improves students (Level 2).
- Negative reasoning helps. Adding a contrastive objective to learn from *incorrect* reasoning provides a valuable signal (Level 3).
- **Distilling from structure maximizes accuracy.** When MAGDI distills from the first 3 levels *and the structure* of a MAG, the student achieves the highest accuracy (Level 4).
- MAGDI balances performance with efficiency. MAGDI-distilled models reduce the number of tokens predicted by up to 9x while outperforming all single-teacher distillation baselines.

Building on these results, we further analyze MAGDI along the following axes: (1) Generalizability. MAGDI can be used to produce a unified joint multi-task learning model that performs well on multiple domains at once and also generalizes well to held-out datasets not seen during training. (2) Scalability. MAGDI scales positively with the size and strength of the base student model. (3) Diversity. The output diversity resulting from our multi-teacher training improves self-consistency (Wang et al., 2023), an inference-time ensemble method relying on diverse model answers.

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